

國立中山大學

NATIONAL SUN YAT-SEN UNIVERSITY

線性代數 (二)

MATH 104A / GEAI 1209A: Linear Algebra II

第一次期中考

March 19, 2025

Midterm 1

姓名 Name : \_\_\_\_\_

學號 Student ID # : \_\_\_\_\_

Lecturer: Jephian Lin 林晉宏

Contents: cover page,  
**5 pages** of questions,  
score page at the end

To be answered: on the test paper

Duration: **110 minutes**

Total points: **20 points** + 2 extra points

**Do not open this packet until instructed to do so.**

Instructions:

- Enter your **Name** and **Student ID #** before you start.
- Using the calculator is not allowed (and not necessary) for this exam.
- Any work necessary to arrive at an answer must be shown on the examination paper. Marks will not be given for final answers that are not supported by appropriate work.
- Clearly indicate your final answer to each question either by **underlining it or circling it**. If multiple answers are shown then no marks will be awarded.
- Please answer the problems in English.

1. Let  $A$  be a  $3 \times 3$  matrix whose rows are  $\mathbf{x}, \mathbf{y}, \mathbf{z}$ . Suppose  $\det(A) = 5$ .
  - (a) [1pt] Let  $B$  be the  $3 \times 3$  matrix whose rows are  $\mathbf{x}, 3\mathbf{x} + \mathbf{y}, \mathbf{z}$ . Find  $\det(B)$ .
  
  - (b) [1pt] Let  $B$  be the  $3 \times 3$  matrix whose rows are  $\mathbf{x}, \mathbf{y}, 5\mathbf{z}$ . Find  $\det(B)$ .
  
  - (c) [1pt] Let  $B$  be the  $3 \times 3$  matrix whose rows are  $\mathbf{z}, \mathbf{y}, \mathbf{x}$ . Find  $\det(B)$ .
  
  - (d) [1pt] Let  $B$  be the  $3 \times 3$  matrix whose rows are  $\mathbf{y}, \mathbf{z}, \mathbf{x}$ . Find  $\det(B)$ .
  
  - (e) [1pt] Let  $B$  be the  $3 \times 3$  matrix whose rows are  $\mathbf{x} + \mathbf{y}, \mathbf{y} + \mathbf{z}, \mathbf{z} + \mathbf{x}$ . Find  $\det(B)$ .

2. Find the determinant of

$$A = \begin{bmatrix} 1 & 2 & 0 & -3 & 2 \\ -3 & -5 & -2 & 12 & -7 \\ -3 & -6 & 1 & 9 & -9 \\ 16 & 26 & 14 & -68 & 30 \\ -9 & -16 & -3 & 34 & -21 \end{bmatrix}.$$



6. [5pt] Mathematical essay: Write a few paragraphs to introduce the *permutation expansion*.

Your score will be based on the following criteria.

- The definition is clear.
- Some sentences are added to explain the definition.
- Examples or pictures are included to help understanding.
- The sentences are complete.

7. [extra 2pt] Let

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix}.$$

Find  $\det(A)$ .

**[END]**

Page	Points	Score
1	5	
2	5	
3	5	
4	5	
5	2	
Total	20 (+2)	